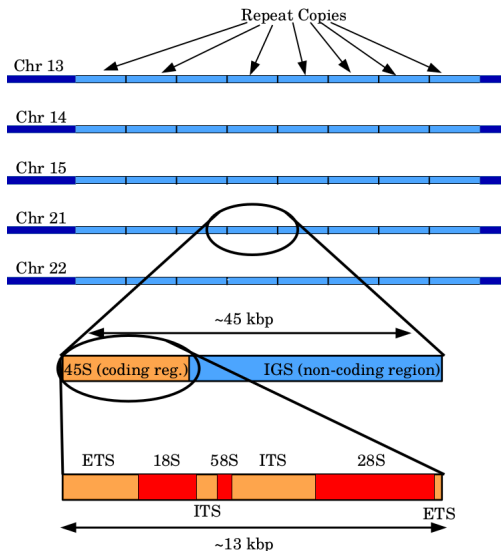


# A combinatorial approach for reconstructing rDNA repeats

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# Introduction

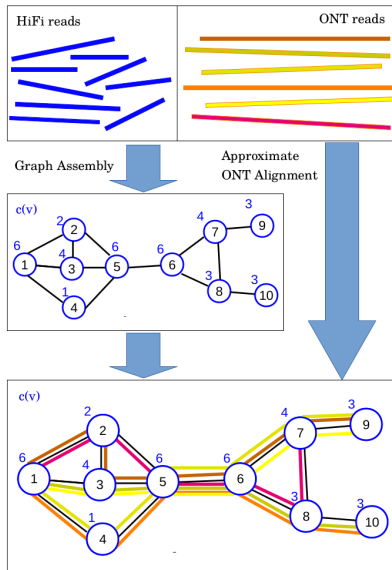


- Combinatorial method for resolving the individual rDNA repeat copies from any given human sample
- Assembly of the rDNA repeat copies from six samples → CHM13, HPRC (Human Pangenome Reference Consortium)
- CHM13: Comparison with T2T assembly → Appendix

## Related Work

- Telomere-to-telomere (T2T) Consortium [1] → CHM13 reference genome, rDNA assembly
- Methods for graph-based assembly and sequence-to-graph-alignment → MBG [2] and GraphAligner [3]
- Viral quasispecies assembly by Baaijens et al. [4] → We use a similar optimization approach

## Model: Preprocessing



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 OPTIMAL REPEAT SELECTION
 

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**Input:** An undirected graph  $G = (V, E)$ .  
 A multiset of reads  $R_{Aln} = \{ra_1, ra_2, \dots, ra_n\}$ , where each read is a path in  $G$ .  
 A value  $c(v) \in \mathbb{R}$  for each  $v \in V$ .  
 A constant  $c_{avg} \in \mathbb{R}$ .  
 A weight  $w(v) \in \mathbb{R}$  for each  $v$ .  
 A fixed value  $k \in N$ , denoting the number of paths to select.

**Output:** A subset  $R_{Opt} \subseteq R_{Aln}$  with  $|R_{Opt}| = k$ , such that

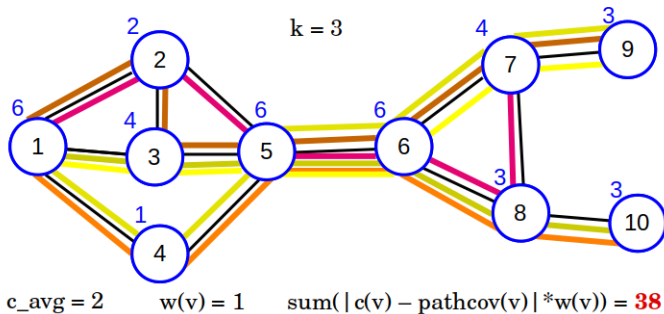
$$\sum_{v \in V} |c(v) - pathcov(v)| \cdot w(v)$$

is minimized.

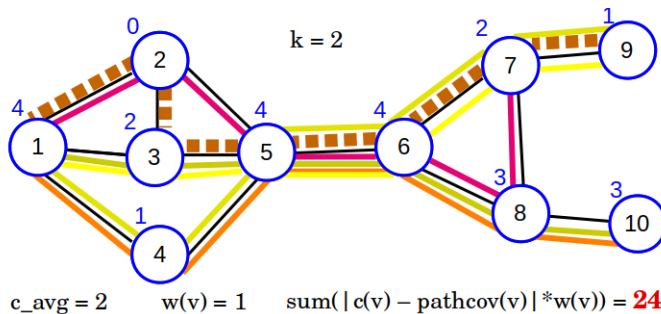
For each node  $v \in V$ ,  $pathcov(v) = c_{avg} \cdot |\{ra \in R_{Opt} | v \in ra\}|$ .

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## Model: Example

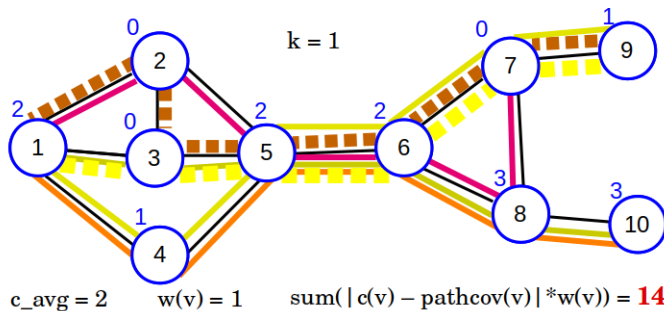


## Model: Example

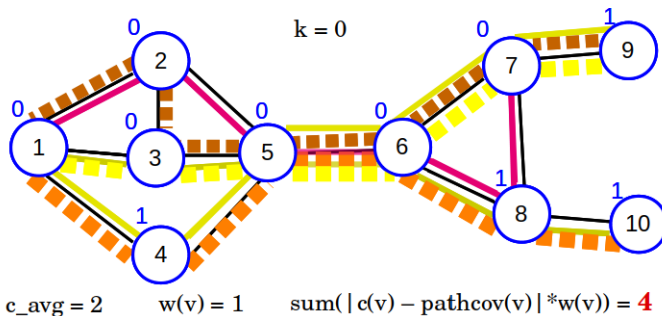




## Model: Example

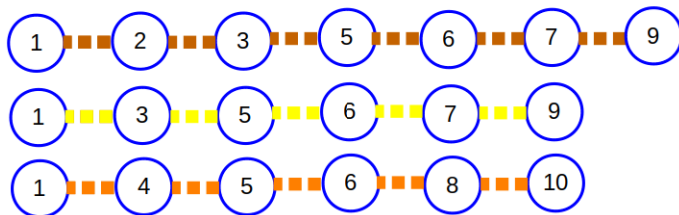


## Model: Example



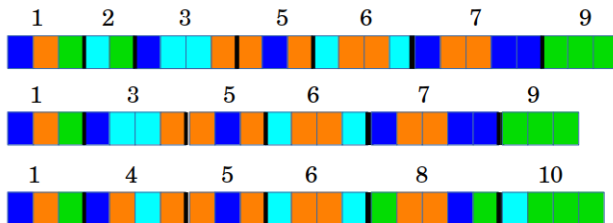
## Model: Example

Chosen paths:



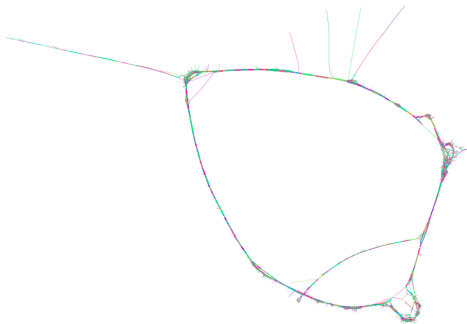
## Model: Example

Reconstructed Repeats:



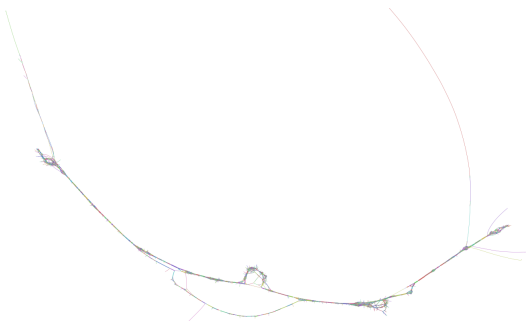
# Results: CHM13

- Assembly graph



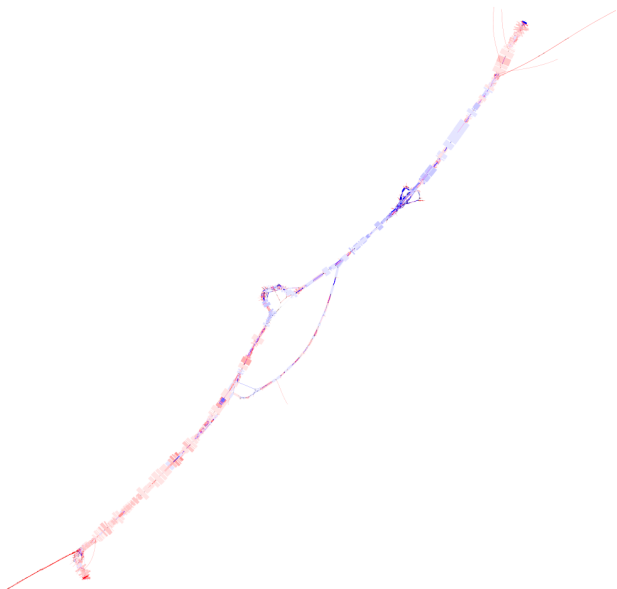
# Results: CHM13

- Assembly graph



## Results: CHM13

- Over- and underexplanation of coverage by the model



## Results: CHM13

- Repeat sequences from our model, aligned against the canonical rDNA unit KY962518.1





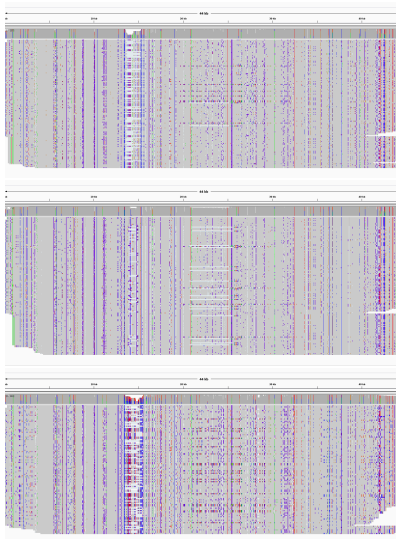
## Results: HPRC samples

- Assembly of five samples from the Human Pangenome Reference Consortium
- Some preprocessing choices were different compared to CHM13

Sample	R <sub>AIn</sub>	k	c <sub>avg</sub>	Coverage pre-run	Coverage post-run	Explained coverage	ILP runtime	Gap
HG01258	902	157	22	6843835.8	2523671.1	63.1%	7500s	0.02%
HG01361	689	112	27	5798865.7	2479513.9	57.2%	485s	< 0.01%
HG01952	1485	152	27	7601852.0	2801403.8	63.1%	1826s	< 0.01%
HG02257	397	124	21.5	4691861.1	1801916.7	61.6%	55s	< 0.01%
HG03579	811	230	33	15272751.3	6014994.3	60.6%	544s	< 0.01%

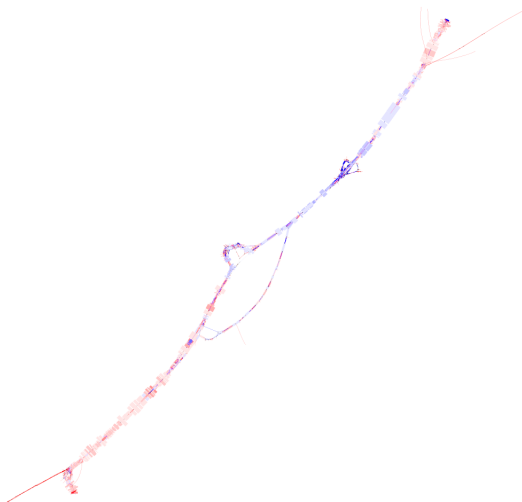
## Results: HPRC samples

- Example: HG01258, HG01952, HG02257
- Significant differences in some regions → Junction between coding region and IGS, central part of IGS



## Future Challenges

- Room for improvement → Improperly explained coverage



# Future Challenges

- Improving the model
- Resolving the order of the copies on the genome
- Haplotyping the copies

Thank you for your attention!

## Literature



Sergey Nurk et al. *The complete sequence of a human genome*. Science 376 (6588 2022), pp. 44–53. DOI: [10.1126/science.abj6987](https://doi.org/10.1126/science.abj6987).



Mikko Rautiainen and Tobias Marschall. *MBG: Minimizer-based sparse de Bruijn Graph construction*. Bioinformatics 37 (16 2021), pp. 2476–2478. DOI: [10.1093/bioinformatics/btab004](https://doi.org/10.1093/bioinformatics/btab004).



Mikko Rautiainen and Tobias Marschall. *GraphAligner: rapid and versatile sequence- to-graph alignment*. Genome Biology 21 (253 2020). DOI: [10.1186/s13059-020-02157-2](https://doi.org/10.1186/s13059-020-02157-2).



Jasmijn A. Baaijens et al. *Full-length de novo viral quasispecies assembly through variation graph construction*. In: Bioinformatics 35 (24 2019), pp. 5086–5094. DOI: [10.1093/bioinformatics/btz443](https://doi.org/10.1093/bioinformatics/btz443).

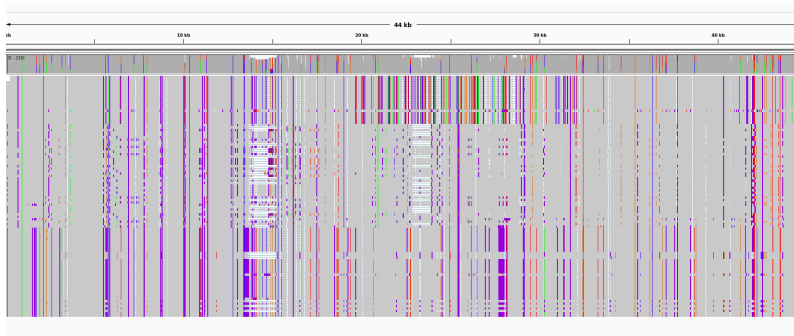
## Appendix: Comparison with T2T assembly

- Repeat sequences from our model, aligned against the canonical rDNA unit KY962518.1



## Appendix: Comparison with T2T assembly

- Repeat sequences from the T2T assembly, aligned against the canonical rDNA unit KY962518.1





## Appendix: Comparison with T2T assembly

- Idea: Compute edit distance for all pairs of copies from both assemblies
- Find a minimum-weight perfect matching
- Only compute pairs that are similar enough  $\rightarrow$  Cutoff  $c$

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### COMPLETE BIPARTITE EDIT DISTANCE GRAPH

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**Input:** Two sets of strings  $S_1, S_2$ .

A cutoff  $c \in \mathbb{N}$ .

**Output:** A complete bipartite graph  $G = (V_1, V_2, E)$  where the nodes in  $V_1, V_2$  correspond to the sequences in  $S_1, S_2$ , and a function  $f : E \rightarrow \mathbb{N}$ , such that

$$\forall e = \{v_i, v_j\} \in E : f(e) = \begin{cases} d(s_i, s_j) & \text{if } d(s_i, s_j) \leq c \\ \max\{|s_i|, |s_j|\} & \text{else} \end{cases}$$


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## Appendix: Comparison with T2T assembly

- The sets of copies differ considerably
- MWPM: Only 53 pairs of repeats with an edit distance  $\leq 4500$
- For 54 copies from RS model, there is at least one similar copy in the T2T set
- For 215 copies vice versa
- Our copies vary more than the T2T copies → Is this accurate?

## Appendix: Comparison with T2T assembly

- Idea: Retrace unique feature of each repeat copy in the HiFi reads → Find SHORTEST IDENTIFIERS
- Homopolymer compression for cleaner results

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### SHORTEST IDENTIFIERS

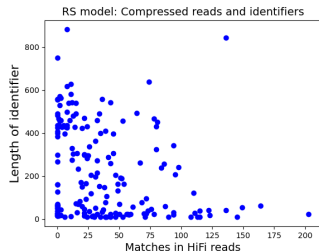
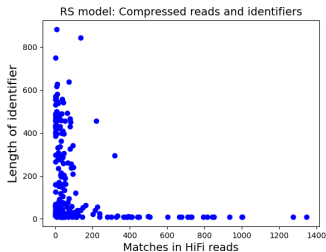
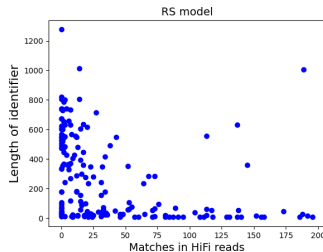
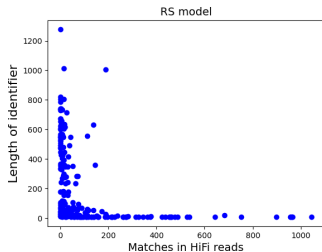
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**Input:** A set of strings  $S = \{s_0, s_1, \dots, s_n\}$ .

**Output:** For each  $s_i \in S$ , the shortest substring  $s_i^*$  of  $s_i$  that (1) Occurs only once in  $s_i$ , and (2) Occurs in no other string in  $S$ .

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## Appendix: Comparison with T2T assembly



## Appendix: Comparison with T2T assembly

